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Airside characteristics of heat, mass transfer and pressure drop for heat exchangers of tube-in hydrophilic coating wavy fin under dehumidifying conditions

Xiaokui Ma^a, Guoliang Ding^{a,*}, Yuanming Zhang^a, Kaijian Wang^b

^a Institute of Refrigeration and Cryogenics, Shanghai Jiaotong University, No. 800 Dongchuan Road, Shanghai 200240, China
^b Fujitsu General Institute of Air-Conditioning Technology Limited, 1116 Suenaga, Takatsu-Ku, Kawasaki 213-8502, Japan

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ABSTRACT

The airside heat, mass and momentum transfer characteristics of seven wavy fin-and-tube heat exchangers with hydrophilic coating under dehumidifying conditions were experimented. The test inlet air dry bulb temperatures were 20, 27 and 35 °C, the inlet relative humidity were 50%, 60%, 70% and 80%, and the air velocity were 0.5, 1.0, 2.0, 3.0 and 4.0 m s⁻¹. The test results indicate that both the Colburn j_m factor and the Colburn j_h factor decrease with the increase of fin pitch, and this phenomenon becomes more and more pronounced as Reynolds number decreases. The friction factor is very sensitive to the change of fin pitch, and the friction factor shows a cross-over phenomenon as fin pitch changes. The Colburn j_h factor decreases and the Colburn j_m factor increases when the number of tube rows increases, while the friction performance is insensitive to the change of the number of tube rows. The effects of inlet relative humidity on the heat transfer and friction performance can be omitted, but the Colburn j_m factor decreases with the increase of the inlet relative humidity. The predictive ability of the available stateof-the-art heat transfer and pressure drop correlations was evaluated with the experiment data of the present study. The new heat, mass and momentum transfer correlations were proposed to describe the present test results according to the multiple linear regression technique. The mean deviations of the proposed j_h, j_m and f correlations are 6.3%, 8.9% and 7.9%, respectively. Comparing to published data reduction method, the process line on psychrometric chart of fin-and-tube heat exchanger for partially wet conditions and more accurate overall heat transfer coefficient equation are put forward in this paper.

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1. Introduction

Fin-and-tube heat exchangers are essential components in air conditioning and refrigeration systems. Enhanced surface are often employed to effectively improve the overall performance of the fin-and-tube heat exchangers. Wavy fins are among the very popular enhanced fin patterns. The wavy surface can lengthen the path of the airflow and cause better airflow mixing, resulting in higher heat transfer performance.

When the surface temperature is below the dew point temperature of incoming air, simultaneous heat and mass transfer occurs on the fin surface, and condensate water is formed. The airflow across the heat exchanger may interact with the condensate water which makes the flow pattern become very complicated. As a result, significant change of the heat/mass transfer and friction characteristics is likely to occur under dehumidifying conditions. However, experimental data for dehumidifying conditions are comparatively few. Mirth and Ramadhyani [1,2] presented test results for five smooth wavy fin patterns. Their results showed that the Nusselt numbers were very sensitive to the change of inlet air dew point temperature, and the Nusselt number decreases with the increase of inlet air dew point temperature. Wang et al. [3], Lin et al. [4] and Pirompugd et al. [5] analyzed the effects of the number of tube rows, fin pitch and tube size, etc. on airside performance for herringbone wavy fin patterns in wet conditions, and developed their airside heat transfer and friction correlations.

The above-mentioned researches are focused on the wavy fin without hydrophilic coating. The condensate water may adhere as droplets on the fin surfaces without hydrophilic coating, and this phenomenon will cause bridging between the fins and increase airside pressure drop. Furthermore, the condensate water may corrode aluminum fins, and produce corrosion problems. A solution to solve this problem is to add hydrophilic coating on the aluminum fins. The hydrophilic coating can effectively improve the condensate water drainage and decrease airside pressure drop. Information on the effects of hydrophilic coating on the thermal/hydraulic performances of the fin-and-tube heat exchangers is also rare in open literatures. Mimaki [6] showed that the airside pressure drop of the coils under wet conditions was reduced up to 20–50% by using hydrophilic coated fins.

^{*} Corresponding author. Tel.: +86 21 34206378; fax: +86 21 34206814. *E-mail address:* glding@sjtu.edu.cn (G. Ding).

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Nomenclature

а	coefficient defined by Eq. (A7)
A_1	outside surface area of tubes (m ²)
A_2	surface area of fin (m ²)
$A_{\rm fr}$	frontal area (m ²)
A _{min}	minimum free-flow area (m ²)
A_0	total airside surface area (m^2)
b	coefficient defined by Eq. (A7)
C_n	specific heat $(kg^{-1}K^{-1})$
D_c	fin collar outside diameter (m)
f	friction factor
, Fn	fin pitch (m)
F_{s}	fin spacing (m)
Ğ	mass flux of the air based on the minimum flow area
C C	$(\text{kg m}^{-2} \text{ s}^{-1})$
$h_{\rm m}$	mass transfer coefficient (kg m ^{-2} s ^{-1})
h_s	sensible heat transfer coefficient (W $m^{-2} K^{-1}$)
i	enthalpy (kJ kg $^{-1}$)
i_{fg}	saturated water vapor enthalpy (kJ kg $^{-1}$)
I ₀	modified Bessel function solution of the first kind, order
-	0
I_1	modified Bessel function solution of the first kind, order
	1
$j_{ m h}$	Colburn heat transfer factor
$j_{\rm m}$	Colburn mass transfer factor
k	thermal conductivity (W m ⁻¹ K ⁻¹)
K ₀	modified Bessel function solution of the second kind, or-
	der 0
K_1	modified Bessel function solution of the second kind, or-
	der 1
Le	Lewis number
т	mass flow rate (kg s ^{-1})
m^*	coefficient defined by Eq. (A15)
Μ	condensate rate (kg s $^{-1}$)
$M_{ m fb}$	coefficient defined by Eq. (A3)
M^{*}	coefficient defined by Eq. (A2)
Ν	number of longitudinal tube rows
P_l	longitudinal tube pitch (m)

Pr	Prandtl number
P_t	transverse tube pitch (m)
ΔP	pressure drop of airside (Pa)
Q	average heat transfer rate (W)
Qs	sensible heat transfer rate (W)
Q_1	latent heat transfer rate (W)
r	fin radius (m)
<i>Re</i> _{Dc}	Reynolds number based on tube collar diameter
RH	relative humidity
Sc	Schmidt number
Т	temperature (K)
T_a^*	coefficient defined by Eq. (A4)
Ň	velocity (m s ^{-1})
W	humidity ratio of moist air $(kg kg^{-1})$
Greek syr	nbols
β	coefficient defined by Eq. (A5)
δ	fin thickness (m)
$\eta_{\mathrm{f,h,wet}}$	wet fin efficiency for heat transfer
$\eta_{\mathrm{f,m}}$	fin efficiency for mass transfer
η_{o}	overall surface effectiveness
ξ	boundary line between dry region and wet region
Subscript	c
Subscript.	air
d d	dew point
u drv	dry hulb temperature
f	fin
1 fb	fin base
ft	fin tin
ii ii	inn up
in	inlet
	outer
U OUIT	
out	outiet
5	Saturateu
vv	Walti

Hong [7] presented a fundamental aspect to the hydrophilic coating surfaces. Among the methods of coating the aluminum fins, as documented by Hong and Webb [8], chemical methods are adopted as the main-stream methods. Hong and Webb [9] did researches on enhanced fin-and-tube heat exchangers with and without hydrophilic coating. The results showed that hydrophilic coating would reduce the pressure drop. For wet coils, the hydrophilic coating applied on the louver and wavy fin reduces the wet pressure drop to 45% and 15% at 2.5 m s⁻¹ frontal air velocity, respectively. The airside performance comparison of plain, louver, and slit fin-and-tube heat exchangers with and without hydrophilic coating were examined by Wang et al. [10,11]. The results showed that the heat transfer performance for the hydrophilic coating surface is lower than that for the corresponding uncoated surface tested at the same wet conditions. and the pressure drops for the hydrophilic coated surface are also lower than the corresponding uncoated surfaces.

Until now, no data on the wavy fin-and-tube heat exchangers with hydrophilic coating under wet conditions have been published in open literatures. As a consequence, the main purpose of this study is to present airside heat, mass and momentum transfer performance of wavy fin-and-tube heat exchanger with hydrophilic coating under dehumidifying conditions, which may give helps in design of wavy fin-and-tube heat exchangers.

2. Experimental apparatus

The experimental apparatus is schematically illustrated in Fig. 1, which includes an air flow loop, a water flow loop, a data acquisition system and the test heat exchangers.

The air flow loop is a close type wind tunnel to conduct the air flow through the heat exchanger. The wind tunnel is made of galvanized steel sheet and the test section has a 210 mm \times 210 mm cross-section. A variable speed centrifugal fan (0.75 kW) is used to circulate the air passing through the nozzle chamber, the air conditioner box, the mixing device, the straightener, and the test heat exchanger orderly. The air flow rate measurement is detected by multiple nozzles based on the ASHRAE 41.2 standard [12]. A differential pressure transducer with ±5.0 Pa precision is used to measure the pressure difference across the nozzles. A pressure transducer with ±1.0 kPa precision and a dry bulb and wet bulb temperature transducer with ±0.3 °C precision are used to measure the inlet air conditions of nozzles. The air conditioner box is used to control the temperature and humidity of inlet air, which are allowed ±0.2 °C and ±3% fluctuation range. The test section is insulated with a 15 mm thick standard sheet. A differential pressure transducer with ±0.2 Pa precision is used to measure the pressure difference across the heat exchangers. The dry bulb temperature and relative humidity of the inlet and outlet air are measured by



- Volume flow meter
- 2 Pump
- 3 Thermostat
- 4 Air conditioner box
- 5 Mixer
- 5 Straightener
- 7 Temperature and humidify transducer
- Fin-and-tube heat exchanger
- 9 Video camera
- 10 Pressure difference transducer
- 11 Pressure difference transducer
- 12 Pressure transducer
- 13 Straightener
- 14 Nozzle
- 15 Dry and wet bulb temperature meter
- 16 Variable speed centrifugal fan

Fig. 1. Schematic of experimental setup.

two temperature and humidity transducers with ± 0.1 °C and $\pm 1.4\%$ precision. Six K-type thermocouples with ± 0.1 °C precision welded on the tube surface are used to measure the fin base temperature.

The water flow loop consists of a thermostat, a centrifugal pump and a magnetic flow meter with ± 0.15 L/min precision. The purpose of this loop is to provide the cool capacity of the test heat exchangers. After the water reaches the required temperature, it is pumped out of the thermostat, delivered to the heat exchanger and then returned to the thermostat. The water temperature differences between inlet and outlet of heat exchangers are measured

by two K-type thermocouples with a calibrated accuracy of ± 0.1 °C. All signals are registered by a data acquisition system and finally averaged over the elapsed time.

Seven fin-and-tube heat exchangers for testing are made of aluminum fin and copper tube. Detailed dimensions of the heat exchangers and the fins are shown in Fig. 2. Their detailed configurations are tabulated in Table 1. Fin surface coatings include anti-corrosive layer and hydrophilic layer. The coating material is organic resin, the thickness of anti-corrosive layer and hydrophilic layer is 1.1 μ m and 0.8 μ m, and the static contact angle on the



Air flow direction: From reader into the paper

Fig. 2. Structure dimensions of the tested fin-and-tube heat exchangers.

			-					
No.	$F_{\rm p}~({\rm mm})$	δ (mm)	$D_{\rm c}~({\rm mm})$	$P_{\rm t}({\rm mm})$	P_1 (mm)	$P_{\rm d}~({\rm mm})$	$X_{\rm f}({\rm mm})$	Ν
1	1.2	0.105	7.51	21.0	19.05	1.352	4.625	2
2	1.5	0.105	7.51	21.0	19.05	1.352	4.625	2
3	1.7	0.105	7.51	21.0	19.05	1.352	4.625	2
4	1.4	0.105	10.31	25.4	19.05	1.352	4.625	2
5	1.8	0.105	10.31	25.4	19.05	1.352	4.625	2
6	1.5	0.105	7.51	21.0	19.05	1.352	4.625	3
7	1.4	0.105	10.31	25.4	19.05	1.352	4.625	3

 Table 1

 Geometric dimension of the test fin-and-tube heat exchangers.

*Note: D*_c is the tube outside diameter (including collar thickness) after expansion.

coated fin surface is 10°–20° initially. Coating process chart of fin is shown in Fig. 3.

Condensation phenomena on the fin surface are recorded by a video camera put at the outlet of air. Total 23 test conditions are listed in Table 2. Experiment uncertainties are reported according to the analysis method proposed by Moffat [13], and the maximum error of the Colburn j_h factor and Fanning f factor are ±10.2% and ±9.4%, respectively. The detailed analysis results are tabulated in Table 3.

3. Data reduction

3.1. Heat transfer data

The reduction process is based on the Threlkeld [14] method. The Threlkeld method is an enthalpy-based reduction method. Some important reduction procedures of the original Threlkeld method are described as follows:

The total heat transfer rate used in the calculation is the mathematical average of Q_a and Q_w , namely,

$$Q_{a} = m_{a}(i_{a,in} - i_{a,out}) \tag{1}$$

 $Q_{\rm w} = m_{\rm w} C_{p,{\rm w}}(T_{{\rm w},{\rm out}-T_{{\rm w},{\rm in}}}) \tag{2}$

$$Q = (Q_a + Q_w)/2 \tag{3}$$

In the experiments, only those data that satisfy the ASHRAE 33-78 [15] requirements (namely, the energy balance conditions, $|Q_w - Q|/Q \leq 0.05$) are considered in the final analysis.

The overall heat transfer coefficient $(U_{o,w})$ based on the enthalpy potential is given as follows:

$$Q = U_{o,w} A_0 \Delta i_m F \tag{4}$$

where *F* is the correction factor accounting for a single-pass, crossflow heat exchanger and Δi_m is the mean enthalpy difference for counter flow coil.

$$\Delta i_{\rm m} = i_{\rm a,m} - i_{\rm r,m} \tag{5}$$

According to Bump [16] and Myers [17], for the counter flow configuration, the mean enthalpy difference is

$$i_{a,m} = i_{a,in} + \frac{i_{a,in} - i_{a,out}}{\ln\left(\frac{i_{a,in} - i_{r,out}}{i_{a,out} - i_{r,in}}\right)} - \frac{(i_{a,in} - i_{a,out})(i_{a,in} - i_{r,out})}{(i_{a,in} - i_{r,out}) - (i_{a,out} - i_{r,in})}$$
(6)

$$i_{r,m} = i_{r,out} + \frac{i_{r,out} - i_{r,in}}{\ln\left(\frac{i_{a,in} - i_{r,out}}{i_{a,out} - i_{r,in}}\right)} - \frac{(i_{r,out} - i_{r,in})(i_{a,in} - i_{r,out})}{(i_{a,in} - i_{r,out}) - (i_{a,out} - i_{r,in})}$$
(7)

According to the definition of wet fin efficiency by Threlkeld [14] based on the enthalpy difference, Myers [17] reduced the overall heat transfer coefficient related to the individual heat transfer resistance as follows:

$$\frac{1}{U_{\rm o,w}} = \frac{b'_{\rm r}A_0}{h_{\rm i}A_{\rm p,i}} + \frac{b'_{\rm p}A_0\ln\left(\frac{D_{\rm c}}{D_{\rm i}}\right)}{2\pi k_{\rm p}L_{\rm p}} + \frac{1}{h_{\rm o,w}\left(\frac{A_{\rm p,o}}{b'_{\rm w,s}A_0} + \frac{\eta_{\rm f,wet}A_{\rm f}}{b'_{\rm w,s}A_0}\right)}$$
(8)

where



Fig. 3. Coating process of fin surface.

Table 2

The test conditions of experiment.

No.	$T_{\rm a,in}/{\rm ^oC}$	RH _{in} /%	$V/(m s^{-1})$	$T_{\rm w,in}/^{\rm o}C$
1	20	50	0.5	6
2	20	50	1.0	6
3	20	50	2.0	6
4	27	50	1.0	6
5	27	60	1.0	6
6	27	70	1.0	6
7	27	80	1.0	6
8	27	50	0.5	12
9	27	50	1.0	12
10	27	50	2.0	12
11	27	50	3.0	12
12	27	50	4.0	12
13	35	50	0.5	12
14	35	50	1.0	12
15	35	50	2.0	12
16	35	50	3.0	12
17	35	50	4.0	12
18	27	60	1.0	12
19	27	70	1.0	12
20	27	80	1.0	12
21	27	60	1.0	18
22	27	70	1.0	18
23	27	80	1.0	18

Table 3		
Summary	of estimated	uncertainties.

Parameter	Uncertainty		Parameter	Uncertainty	
	Min (%)	Max (%)		Min (%)	Max (%
m _a	±0.9	±1.8	h _s	±6.0	±8.4
m _w	±1.5	±2.5	h _m	±5.1	±7.8
Q_a	±1.8	±3.9	$j_{\rm h}$	±6.9	±10.2
Q_w	±2.5	±5.0	j _m	±6.3	±11.3
ΔP	±0.1	±4.0	f	±3.7	±9.4

$$h_{\mathrm{o,w}} = \frac{1}{\frac{C_{p,a}}{b'_{\mathrm{w,m}}h_{\mathrm{c,o}}}} + \frac{y_{\mathrm{w}}}{k_{\mathrm{w}}} \tag{9}$$

 y_w in Eq. (9) is the thickness of the water film, and was proposed as 0.005 in. by Myers [17]. In practice, (y_w/k_w) accounts for only 0.5–5% compared to $(C_{p,a}/b'_{w,m}h_{c,o})$, and has often been neglected by previous investigators. As a result, this term is not included in the final analysis.

In Eq. (8) there are four quantities $(b'_{w,m}, b'_{w,p}, b'_{p}, and b'_{r})$ involving enthalpy-temperature ratios that must be evaluated. The quantities of b'_{p} and b'_{r} can be calculated as

$$b'_{\rm r} = \frac{i_{\rm s,p,i,m} - i_{\rm r,m}}{T_{\rm p,i,m} - T_{\rm r,m}}$$
(10)

$$b'_{\rm p} = \frac{i_{\rm s,p,o,m} - i_{\rm s,p,i,m}}{T_{\rm p,o,m} - T_{\rm p,i,m}} \tag{11}$$

The $b'_{w,p}$ and $b'_{w,m}$ are defined as the slope of saturated enthalpy curve evaluated at the outer mean water film temperature at the base surface and the fin surface by Threlkeld [14]. However, according to the Threlkeld's analysis method [14], $b'_{w,p}$ and $b'_{w,m}$ should be defined as the slope of saturated enthalpy curve evaluated at the outside surface temperature of tube and at the fin surface mean temperature, and this definition is more appropriate. Evaluation of $b'_{w,m}$ requires a trial and error procedure, for the trial and error procedure, $i_{s,w,m}$ must be calculated using the following equation:

$$i_{s,w,m} = i_{a,m} - \frac{C_{p,a}h_{o,w}\eta_{f,wet}}{b'_{w,p}h_{c,o}} \left(1 - U_{o,w}A_o \left\lfloor \frac{b'_r}{h_i A_{p,i}} + \frac{b'_p \ln\left(\frac{D_c}{D_i}\right)}{2\pi k_p L_p} \right\rfloor\right) (i_{a,m} - i_{r,m})$$
(12)

Wang et al. [18] also used Eq. (8) in their research on fin-andtube heat exchanger under dehumidifying conditions. Threlkeld [14] made a approximation $b'_{f,b} = b'_{w,m}$ during the definition of the wet fin efficiency, and the equation proposed by Threlkeld is as follows:

$$\eta_{\rm f,wet} = \frac{i_{\rm a} - i_{\rm f,m}}{i_{\rm a} - i_{\rm f,b}} \tag{13}$$

When the approximation is removed, the more accurate definition of the wet fin efficiency should be as follows:

$$\eta_{\rm f,wet} = \left(\frac{i_{\rm a} - i_{\rm f,m}}{i_{\rm a} - i_{\rm f,b}}\right) \frac{b_{\rm f,b}'}{b_{\rm w,m}'} \tag{14}$$

where the value of $b'_{f,b}$ is the slope of saturated enthalpy curve evaluated at the fin base temperature. Because the outside surface temperature of tube can be equal to the fin base temperature approximatively, we make the approximation $b'_{f,b} = b'_{w,p}$, and more accurate overall heat transfer coefficient can be gotten as follows:

$$\frac{1}{U_{o,w}} = \frac{b'_{r}A_{o}}{h_{i}A_{p,i}} + \frac{b'_{p}A_{o}\ln\left(\frac{D_{c}}{D_{i}}\right)}{2\pi k_{p}L_{p}} + \frac{b'_{w,p}A_{o}}{h_{o,w}(A_{p,o} + \eta_{f,wet}A_{f})}$$
(15)

The tube side heat transfer coefficient, h_i is evaluated from the Gnielinski correlation [19],

$$h_{\rm i} = \frac{(f_{\rm i}/2)(Re_{\rm Di} - 1000)Pr}{1.07 + 12.7\sqrt{f_{\rm i}/2}\left(Pr^{2/3} - 1\right)} \cdot \frac{k_{\rm i}}{D_{\rm i}}$$
(16)

and the friction factor f_i is

$$f_{\rm i} = \frac{1}{\left(1.58\ln Re_{\rm Di} - 3.28\right)^2} \tag{17}$$

where

$$Re_{\rm Di} = (\rho_{\rm w} V_{\rm w} D_{\rm i})/\mu_{\rm w} \tag{18}$$

For the wet fin efficiency, Wang et al. [18] derived the corresponding formula by the equivalent circular area method

$$\eta_{\rm f,wet} = \frac{2r_{\rm i}}{M_{\rm T}(r_{\rm o}^2 - r_{\rm i}^2)} \times \left[\frac{K_1(M_{\rm T}r_{\rm i})I_1(M_{\rm T}r_{\rm o}) - I_1(M_{\rm T}r_{\rm i})K_1(M_{\rm T}r_{\rm o})}{K_0(M_{\rm T}r_{\rm i})I_1(M_{\rm T}r_{\rm o}) + K_1(M_{\rm T}r_{\rm o})I_0(M_{\rm T}r_{\rm i})} \right]$$
(19)

where

$$M_{\rm T} = \sqrt{\frac{2h_{\rm o,w}}{k_{\rm f}\delta_{\rm f}}} \tag{20}$$

But Eq. (19) can only be used in fully wet conditions. For partially wet conditions, the use of Eq. (19) will bring big error. In this regard, the authors analyzed wet fin efficiency $\eta_{\rm f,wet}$, and listed the detailed reduction process and comparison with other fin efficiency correlations in the literature. Ma [20]. The calculation correlations of wet fin efficiency $\eta_{\rm f,wet}$ are listed in Appendix A.

The heat transfer performance is in terms of the Colburn j_h factor, i.e.,

$$j_{\rm h} = \frac{h_{\rm c,o}}{G_{\rm c}C_{p,\rm a}} P r^{2/3} \tag{21}$$

where

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$$G_{\rm c} = \frac{m_{\rm a}}{A_{\rm min}} \tag{22}$$

3.2. Mass transfer data

For the cooling and dehumidifying of moist air by a cold surface, the heat and mass transfer can be described by the process line equation from Threlkeld [14]:

$$\frac{di_{a}}{dW_{a}} = R \frac{(i_{a} - i_{s,w})}{(W_{a} - W_{s,w})} + (i_{fg} - 2501R)$$
(23)

where R represent the ratio of sensible heat transfer characteristics to the mass transfer performance,

$$R = \frac{h_{\rm c,o}}{h_{\rm d,o}C_{\rm p,a}} \tag{24}$$

However, for the fin-and-tube heat exchanger, Eq. (23) does not correctly describe the dehumidification process on the psychometric chart because the saturated air enthalpy $(i_{s,w})$ at the mean temperature at the fin surface is different from that at the fin base. In this regard, Pirompugd [5] put forward a modification process line on the psychometric chart corresponding to the fin-and-tube heat exchanger.

$$\frac{(i_{a,in} - i_{a,out})}{(W_{a,in} - W_{a,out})} = R \cdot \frac{(i_{a,m} - i_{s,p,o,m}) + (\varepsilon - 1)(i_{a,m} - i_{s,w,m})}{(W_{a,m} - W_{s,p,o,m}) + (\varepsilon - 1)(W_{a,m} - W_{s,w,m})}$$
(25)



Fig. 4. Effect of the parameters on the airside heat and momentum transfer performance. (a) Fin pitch, (b) number of rows and (c) inlet relative humidity.

where

$$\varepsilon = \frac{A_0}{A_{\rm p,o}} \tag{26}$$

But Eq. (25) is only suitable for fully wet conditions. In this paper, the process line on psychrometric chart of fin-and-tube heat exchanger for partially wet conditions is put forward. The derivation is as follows:

From the energy balance of the dehumidification one can arrive at the following expression

$$m_{\rm a}(i_{\rm a,in} - i_{\rm a,out}) = \frac{h_{\rm o,w}}{b'_{\rm w,p}} (A_{\rm p,o} + \eta_{\rm f,wet} A_{\rm f})(i_{\rm a,m} - i_{\rm s,p,o,m})$$
(27)

Conservation of water condensate gives

$$m_{a}(W_{a,in} - W_{a,out}) = h_{d,o}[A_{p,o}(W_{a,m} - W_{s,p,o,m}) + A_{f,wet}(W_{a,m} - W_{s,w,m})]$$
(28)

Dividing Eq. (27) by Eq. (28) yields

$$\frac{(i_{a,in} - i_{a,out})}{(W_{a,in} - W_{a,out})} = R \cdot \frac{b'_{w,m}}{b'_{w,p}} \cdot \frac{(A_{p,o} + \eta_{f,wet}A_f)(i_{a,m} - i_{s,p,o,m})}{A_{p,o}(W_{a,m} - W_{s,p,o,m}) + A_{f,wet}(W_{a,m} - W_{s,w,m})}$$
(29)

The mass transfer performance is in terms of the Colburn $j_{\rm m}$ factor, i.e.,



Fig. 5. Effect of the parameters on the airside mass transfer performance. (a) fin pitch (b) number of rows (c) inlet relative humidity.

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$$j_{\rm m} = \frac{h_{\rm d,o}}{G_{\rm c}} S c^{2/3} \tag{30}$$

An algorithm for solving the Colburn j_h factor and Colburn j_m factor is given as follows:

- (1) Based on the measurement data, calculate the total heat transfer rate Q using Eq. (3).
- (2) Calculate the tube side heat transfer coefficient of h_i using Eq. (16).
- (3) Calculate $i_{a,m}$ by Eq. (6) and $i_{r,m}$ by Eq. (7).
- (4) Calculate $T_{p,i,m}$ and $T_{p,o,m}$.
- (5) Assume a value of *R*.
- (6) Assume a value of $h_{c,o}$.
- (7) Calculate the wet fin efficiency $\eta_{f,wet}$.
- (8) Calculate the b'_{p} and b'_{r} .
- (9) Calculate the overall heat transfer coefficient $U_{o,w}$.
- (10) Assume a value of $T_{w,m}$.
- (11) Calculate $i_{s,w,m}$ by Eq. (12).
- (12) Calculate $T_{w,m}$ from $i_{s,w,m}$.
- (13) If $T_{w,m}$ derived in step (12) is not equal that is assumed in step (10), the calculation steps (10)–(12) will be repeated with $T_{w,m}$ derived in step (12) until $T_{w,m}$ is constant.
- (14) Calculate $h_{c,o}$ from Eq. (15).
- (15) If $h_{c,o}$ derived in step (14) is not equal to that assumed in step (6), the calculation steps (6)–(14) will be repeated with $h_{c,o}$ derived in step (14) until $h_{c,o}$ is constant.
- (16) Obtain $W_{s,p,o,m}$ and $W_{s,w,m}$ from $i_{s,p,o,m}$ and $i_{s,w,m}$.
- (17) Calculate *R* using Eq. (25) under fully wet conditions, and calculate *R* using Eq. (29) under partially wet conditions.
- (18) If *R* derived in step (17) is not equal to that assumed in step (5), the calculation steps (5)–(17) will be repeated with *R* derived in step (17) until $h_{c,o}$ is constant.
- (19) Calculate $h_{d,o}$ by Eq. (24).
- (20) Calculate the Colburn j_h factor by Eq. (21) and Colburn j_m factor by Eq. (30).

3.3. Momentum transfer data

The reduction of the Fanning f factor of the heat exchanger is evaluated from the pressure drop equation proposed by Kays and London [21],

$$f = \frac{A_{\min}}{A_0} \frac{\rho_m}{\rho_i} \left[\frac{2\Delta P \rho_i}{G_c^2} - (1 + \sigma^2) \left(\frac{\rho_i}{\rho_o} - 1 \right) \right]$$
(31)

where

$$\tau = \frac{A_{\min}}{A_{fr}} \tag{32}$$

4. Results and discussion

4.1. Analysis on heat and momentum transfer characteristics

Fig. 4(a) shows the effect of the fin pitch on the airside heat transfer and friction characteristics of wavy fin with hydrophilic coating. The ordinates are Colburn $i_{\rm b}$ factors and Fanning f factor, and the abscissa is the Reynolds number based on collar diameter. The inlet air dry bulb temperature is 27 °C, the inlet air relative humidity is 50%, the inlet water temperature is 12 °C, and the number of tube rows is 2. As shown in Fig. 4(a), the Colburn j_h factors decrease with the increase of the fin pitch. This phenomenon is especially pronounced in low Reynolds number region. The trend is different with research results of plain, wavy and louver fin-andtube heat exchanger having a 4-row configuration by Rich [22] and Wang et al. [18,23-26], whatever dry conditions or dehumidifying conditions. But for fin-and-tube heat exchanger having 1-row and 2-row configuration, the research results by Wang et al. [3,27] is similar to that of this paper, so the effect of the fin pitch on the airside heat transfer performance is relative to the number of tube rows. This phenomenon can be further explained by the 3D numerical investigation results obtained by Torikoshi et al. on a 1-row plain fin-and-tube heat exchanger [28]. The results show that the vortex that forms behind the tube can be suppressed and entire flow region can be kept steady and laminar when the fin pitch is small enough. Further increase of the fin pitch would result in a noticeable increase of cross-stream width of the vortex region behind the tube. The detailed explanations for this phenomenon can be found in the research by Wang et al. [27]. Fig. 4(a) also shows that the friction factors show a cross-over phenomenon as fin pitch changes, which is similar with the results under dry conditions [24].



Fig. 6. Validation of existing heat transfer correlations with experiment data.

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Fig. 4(b) depicts the effect of the number of tube rows on the airside performance of wavy fin-and-tube heat exchangers with hydrophilic coating. The ordinates are Colburn $j_{\rm h}$ factors and Fanning *f* factor, and the abscissa is the Reynolds number based on collar diameter. The Colburn *j* factors decrease with the increase of the number of tube rows. This phenomenon is especially pronounced in low Reynolds number region. This trend is similar with the test results of plain fin-and-tube heat exchanger by Rich [29] and Wang et al. [23,27] under dry conditions and it is also similar with the results of plain fin and wavy fin by Wang et al. [3,18] under dehumidifying conditions. The possible explanations of this phenomenon are summarized as follows. The downstream turbulence is deteriorated by the vortices formed behind the tube row, and the downstream turbulence tends to diminish with the increase of the number of tube rows. When the Revnolds number decreases, the vortices behind the tube become more pronounced [23]. Fig. 4(b) also indicates that the friction factors are insensitive to the number of tube row for wavy fin with hydrophilic coating under dehumidifying condition. Because the condensate water can be drained by the hydrophilic coating in time, this phenomenon is very similar with the test results of fin-and-tube heat exchanger under dry conditions [23,24,29]. Wang et al. [3] made the airside performance experimental research of wavy fin-and-tube heat exchanger without hydrophilic coating under dehumidifying condition, and they found that the effect of the number of tube rows on the airside friction characteristic is very sensible. Their result is different from that of this paper, and this difference may be caused by the different dehumidification conditions on the fin surface between the coated fin and uncoated fin. For coated fin, water film will be formed on the fin surface; for uncoated fin, water droplets will be formed on the fin surface. When the fin pitch is close to each other, the droplets adhering to the fin surface may cause the airflow twisting. As humid air flows across the wet coils, the corresponding specific humidity decreases along the direction of the airflow, the local dew point temperatures decrease and the driving potential of mass transfer also decreases. The condensate water rate and twisted airflow may decrease as the number of tube rows increase. As a result, for the uncoated fin, the friction factors decrease with the increase of the number of tube rows; but for the coated fin, this phenomenon does not exist.

Fig. 4(c) shows the effect of the inlet relative humidity on the airside performance of wavy fin-and-tube heat exchanger with hydrophilic coating. The air dry bulb temperature $T_{a,dry} = 27$ °C, the inlet air flow velocity $V_{a,in} = 1.0 \text{ ms}^{-1}$, and the corresponding number of tube rows is 2. As shown in Fig. 4(c), the Colburn *j* factors and the friction factors are relatively insensitive to the change of inlet relative humidity. This is similar with the experimental results of plain fin, slit fin and louver fin by Wang et al. [18,30,31] and is different from the test result by Mirth and Ramadhyani [1,2] and Fu et al. [32]. Wang et al. [18] pointed out that the reason was that they chose different wet fin efficiency calculation equations.

4.2. Analysis on mass transfer characteristic

The effect of the fin pitch, the number of tube rows and the inlet relative humidity on the airside mass transfer characteristic are shown in Figs. 5(a)-(c), respectively. The ordinates are Colburn j_m factor, and the abscissa is the Reynolds number based on collar diameter. Fig. 5(a) shows that the airside mass transfer characteristic of smaller fin pitch is better than that of larger fin pitch. The trend is similar with the results of wavy fin without hydrophilic coating by Pirompugd et al. [5]. Fig. 5(b) indicates that the Colburn j_m factor increases with the increase of the

number of tube row. This phenomenon can be explained by the flow visualization experiments conducted by Yoshii et al. [33] who tested a scale-up model under wet conditions. When humid air flows across the wet coils, the corresponding specific humidity decreases along the direction of the airflow. Hence, the local dew point temperatures also decrease and the driving potential of mass transfer is decreased. Thus, the water condensate rate may be decreased as the number of tube row increases. As a result, the water condensate decreases and the mass transfer performance become well with an increase of the number of tube row. Fig. 5(c) shows that the Colburn j_m factor decreases with the increase of inlet relative humidity. The baddish mass transfer characteristic might be resulted from forming of thicker condensate water film on the fin surface when the inlet relative humidity of air increases.



Fig. 7. Validation of existing mass transfer model with experiment data.



Fig. 8. Validation of existing friction correlations with experiment data.

5. Correlations

5.1. Predictability verification of existing correlations to experimental data

The available airside heat transfer correlations of wavy fin include Webb correlation [34], Kim et al. correlation [35] and Wang et al. correlations [24,36–38] for dry condition, and Wang et al. correlation [3], Lin et al. correlation [4] and Pirompugd et al. correlation [5] for dehumidifying condition. The available airside mass transfer correlation in open literatures is only Pirompugd et al. correlation [5]. All the above mentioned heat and mass transfer correlations were developed on the wavy fin without hydrophilic coating.

Fig. 6(a) depicts comparison of predicted values of dry condition correlations with present experimental data. It shows that both Webb correlation [34] and Kim et al. [35] over-predict the experi-

mental data. Wang et al. [38] indicated that the over-prediction may be attributed to the data-source of Beecher and Fagan [39]. A series of investigation of the wavy patterns based on commercially available samples were conducted by Wang et al. [24,25,36,38]. They presented separated correlations applicable to larger diameter tubes ($D_o = 12.7$, 15.88 mm, before expansion) and smaller diameter tubes ($D_o = 7.94$, 9.53 mm, before expansion). Wang et al. correlation [38] is developed using the experimental data by Wang et al. [25,36,37], and it has the most wide application range for wavy fin-and-tube heat exchanger under dry condition at present. Fig. 6(a) also shows the comparison of predicted values of Wang et al. correlations [38] with present experimental data. It shows that Wang et al. correlation [38] over-predict the experimental data.

Fig. 6(b) shows comparison of the experimental data with predicted values of dehumidifying condition correlations. As shown in



Fig. 9. Comparison of the proposed heat/mass and momentum transfer correlations with experimental data of wavy fin with hydrophilic coating under wet conditions (a) j_h (b) j_m (c) f.

Fig. 6(b), Wang et al. correlation [3] and Pirompugd et al. correlation [5] slightly over-predict the experimental data. The reason may be related to the condensate condition on the fin surface. For wavy fin without hydrophilic coating, the condensate water can exist on the fin surface with the form of droplets, which can act as the effect of "rough surface" and enhance the airside heat transfer. Fig. 6(b) also shows that Lin et al. correlation [4] cannot predict the experimental data satisfactorily, because the experimental object of Lin et al. [4] is single wavy fin instead of wavy fin-and-tube heat exchanger.

Fig. 7 shows comparison of the Pirompugd et al. mass transfer correlation [5] with the experimental data. It shows that the Pirompugd et al. correlation [5] over-predict the experimental data. Possible reason is as follows. For fin without hydrophilic coating, the condensate water droplets will make more space for mass transfer between air and fin surface; but for fin with hydrophilic coating, the condensate water exist on the fin surface with the form of film, which will reduce the mass transfer space and decrease the mass transfer performance.

The available momentum transfer correlations include Wang et al. correlation [24,25,38,39] for dry condition and Wang et al. correlation [3], Lin et al. correlation [4] for dehumidifying condition. Fig. 8 indicates the comparison of the experimental data with the predict value. It shows that momentum transfer correlations for dry condition low-predict the pressure drop characteristic of wavy fin-and-tube heat exchanger with hydrophilic coating under dehumidifying condition. The reason is as follows. Although the condensate water comes into being the film on the fin surface, it can still block the flow of air and increase the airside pressure drop. The comparisons of the experimental data with the predicted value of wet condition correlation are also shown in Fig. 8, which depict that the momentum transfer correlations used for uncoated fin over-predict the experimental data. The reason is that the airside pressure drop raised by water droplets on the uncoated fin surface is bigger than that by water film on the coated fin surface.

Above evaluation show that the available heat, mass and momentum correlations cannot predict the airside heat transfer, mass transfer and pressure drop characteristic of wavy fin-andtube heat exchanger with hydrophilic coating under dehumidifying condition satisfactorily. It is necessary to develop new correlation to describe the airside performance better.

5.2. New correlations development

Based on the experimental data, a multiple linear regression technique in a practical range of experimental data ($350 < Re_{Dc} < 4500$) was carried out, and the appropriate correlation form of j_{h} , j_{m} and f are given as follows:

$$j_{\rm h} = 0.3266 Re_{\rm Dc}^{-0.5435} \left(\frac{P_{\rm t}}{P_{\rm l}}\right)^{0.1399} \left(\frac{F_{\rm p}}{D_{\rm c}}\right)^{-0.7482} N^{-0.6314} \tag{33}$$

$$j_{\rm m} = 2.6915 Re_{\rm Dc}^{-0.9098} \left(\frac{P_{\rm t}}{P_{\rm l}}\right)^{0.6632} \left(\frac{F_{\rm p}}{D_{\rm c}}\right)^{-0.6844} N^{0.0219} \tag{34}$$

$$f = 2.0056 Re_{\rm Dc}^{-0.4935} \left(\frac{P_{\rm t}}{P_{\rm l}}\right)^{-0.3782} \left(\frac{F_{\rm p}}{D_{\rm c}}\right)^{-0.3958} N^{-0.2039}$$
(35)

The applicability ranges for Eqs. (33)–(35) are listed as follows:

 $\begin{array}{l} Re_{Dc} 350-4500 \\ P_t \ 21.0-25.4 \ \text{mm} \\ P_1 \ 19.05 \ \text{mm} \\ D_c \ 7.51-10.31 \ \text{mm} \\ F_p \ 1.2-1.8 \ \text{mm} \\ N \ 2-3 \end{array}$

Table 4

Comparison of the proposed correlation with experimental data.^{a,b}

Deviation	<i>j</i> _h (%)	j _m (%)	f (%)
±10%	78.9	60.9	68.8
±15%	90.6	82.1	85.9
±20%	95.3	92.9	97.7
±25%	99.2	96.9	99.2
Mean deviation	6.3	8.9	7.9

^a Mean deviation = $\frac{1}{M} \left(\sum_{1}^{M} \frac{|\text{Correlation}-Data|}{Data} \right) \times 100\%$.

^b *M*, number of data point.

As shown in Fig. 9, the proposed heat transfer j_h factor correlation, mass transfer j_h factor correlation and momentum transfer ffactor correlation can correlate 90.6%, 82.1% and 85.9% of the test data within ±15% deviation limit, and have a mean deviation of 6.3%, 8.9% and 7.9%, respectively. Detailed comparisons between the proposed correlations and the experimental data are depicted in Table 4.

6. Conclusion

The airside heat, mass and momentum transfer performance of compact wavy fin-and-tube heat exchanger with hydrophilic coating under dehumidifying conditions were presented and discussed in this study. A total of seven fin-and-tube heat exchangers having wavy fin geometry were tested. The following conclusions are obtained:

- The process line on psychrometric chart of fin-and-tube heat exchanger for partially wet conditions and more accurate overall heat transfer coefficient calculation equation are put forward.
- The Colburn j_h factor and the Colburn j_m factor decrease with the increase of the fin pitch. This phenomenon becomes more pronounced at lower Reynolds number, and the friction factor is very sensitive to change in fin pitch. The friction factor shows a cross-over phenomenon as fin pitch changes.
- The Colburn j_h factor decreases with the increase of the number of tube rows, and this phenomenon is more pronounced as Reynolds number decrease. The Colburn j_m factor increases with the increase of the number of tube rows. The friction performance is insensitive to the change of the number of tube rows.
- The effects of inlet relative humidity on the heat transfer and friction performance can be omitted, but the Colburn j_m factor decreases with the increase of the number of tube rows.
- The state-of-the-art heat, mass and momentum transfer correlations to experimental data can not well predict the experimental results.
- The new heat, mass and momentum transfer correlations have been proposed to describe the present test results according to the multiple linear regression technique. The mean deviations of the proposed $j_{\rm h}$, $j_{\rm m}$ and f correlations are 6.3%, 8.9% and 7.9%, respectively.

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Appendix A. Wet fin efficiency calculation

For. fully wet conditions

$$\begin{split} \eta_{\rm f,fullywet} &= \frac{2r_{\rm i}M^*(T_{\rm fb} - T_{\rm a}^*)}{M_{\rm fb}^2(r_{\rm o}^2 - r_{\rm i}^2)(T_{\rm a} - T_{\rm fb})} \\ &\cdot \left[\frac{K_1(M^*r_{\rm o})I_1(M^*r_{\rm i}) - I_1(M^*r_{\rm o})K_1(M^*r_{\rm i})}{K_1(M^*r_{\rm o})I_0(M^*r_{\rm i}) + K_0(M^*r_{\rm i})I_1(M^*r_{\rm o})} \right] \end{split}$$
(A1)

where

$$M^{*^2} = \frac{2h_s}{k_f \delta_f} (1 + b\beta) \tag{A2}$$

$$M_{\rm fb}^2 = \frac{2h_{\rm s}}{k_{\rm f}\delta_{\rm f}} \left(1 + \beta \frac{W_{\rm a} - W_{\rm s,f}}{T_{\rm a} - T_{\rm f}}\right) \tag{A3}$$

$$T_a^* = \frac{T_a + \rho \cdot w_a - u\rho}{1 + b\beta}$$
(A4)

$$\beta = \frac{l_{\rm fg}}{RC_{p,\rm a}} \tag{A5}$$

In the calculation, coefficients *a*, *b* and the fin tip temperature $T_{\rm ft}$ need to be iterated. $T_{\rm ft}$ can be calculated by Eq. (A6). When $T_{\rm fb}$ and $T_{\rm ft}$ are specified, if the fin is totally wet ($T_{\rm ft} \leq T_{\rm a,d}$), the values of *a* and *b* can be readily determined with Eqs. (A7) and (A8). If the fin is partially wet ($T_{\rm fb} \leq T_{\rm a,d} \leq T_{\rm ft}$), the values of *a* and *b* can be determined according to $T_{\rm fb}$ and $T_{\rm a,d}$.

$$T_{\rm f} = T_{\rm a}^* + (T_{\rm fb} - T_{\rm a}^*) \left[\frac{K_1(M^*r_{\rm o})I_0(M^*r) + I_1(M^*r_{\rm o})K_0(M^*r)}{K_0(M^*r_{\rm i})I_1(M^*r_{\rm o}) + K_1(M^*r_{\rm o})I_0(M^*r_{\rm i})} \right]$$
(A6)

$$W_{\rm s,f} = a + bT_{\rm f} \tag{A7}$$

$$W_{s,f} = (3.7444 + 0.3078T_f + 0.0046T_f^2 + 0.0004T_f^3) \times 10^{-3} \quad 0 \le T_f \le 30^{\circ} C$$
(A8)

For. partially wet conditions

$$\begin{split} \eta_{\rm f,partiallywet} &= \frac{2r_{\rm i}M^*}{M_{\rm fb}^2(r_o^2 - r_{\rm i}^2)(T_{\rm a} - T_{\rm fb})} \\ &\times \left\{ \begin{bmatrix} I_1(M^*r_{\rm i})K_0(M^*\zeta) + I_0(M^*\zeta)K_1(M^*r_{\rm i}) \\ I_0(M^*r_{\rm i})K_0(M^*\zeta) - I_0(M^*\zeta)K_0(M^*r_{\rm i}) \end{bmatrix} (T_{\rm fb} - T_{\rm a}^*) \\ &- \begin{bmatrix} I_0(M^*r_{\rm i})K_1(M^*r_{\rm i}) + I_1(M^*r_{\rm i})K_0(M^*r_{\rm i}) \\ I_0(M^*r_{\rm i})K_0(M^*\zeta) - I_0(M^*\zeta)K_0(M^*r_{\rm i}) \end{bmatrix} (T_{\rm dew} - T_{\rm a}^*) \right\} \end{split}$$
(A9)

The parameter ξ in Eq. (A9) is the boundary line between dry region and wet region. It can be determined from the continuity of heat flow at the point separating the dry and wet surfaces.

$$\left. \frac{dT_{\rm f}}{dr} \right|_{r=\xi^-} = \frac{dT_{\rm f}}{dr} \bigg|_{r=\xi^+} \tag{A10}$$

The fin surface temperature distribution at dry region and wet region in Eq. (A10) can be seen as following.

For wet region

$$\begin{split} T_{\rm f} &= T_{\rm a}^* + \left[\frac{I_0(M^*r)K_0(M^*\xi) - I_0(M^*\xi)K_0(M^*r)}{I_0(M^*r)K_0(M^*\xi) - I_0(M^*\xi)K_0(M^*r_{\rm i})} \right] (T_{\rm fb} - T_{\rm a}^*) \\ &+ \left[\frac{I_0(M^*r_{\rm i})K_0(M^*r) - I_0(M^*r)K_0(M^*r_{\rm i})}{I_0(M^*r_{\rm i})K_0(M^*\xi) - I_0(M^*\xi)K_0(M^*r_{\rm i})} \right] (T_{\rm dew} - T_{\rm a}^*) \end{split} \tag{A11}$$

$$\begin{split} \frac{dT_{\rm f}}{dr}\Big|_{r=\xi^-} &= M^* \left[\frac{I_1(M^*\xi)K_0(M^*\xi) + I_0(M^*\xi)K_1(M^*\xi)}{I_0(M^*r_{\rm i})K_0(M^*\xi) - I_0(M^*\xi)K_0(M^*r_{\rm i})} \right] (T_{\rm fb} - T_{\rm a}^*) \\ &- M^* \left[\frac{I_0(M^*r_{\rm i})K_1(M^*\xi) + I_1(M^*\xi)K_0(M^*r_{\rm i})}{I_0(M^*r_{\rm i})K_0(M^*\xi) - I_0(M^*\xi)K_0(M^*r_{\rm i})} \right] (T_{\rm dew} - T_{\rm a}^*) \end{split}$$

$$(A12)$$

For dry region

$$\begin{split} T_{\rm f} &= T_{\rm a} + (T_{\rm dew} - T_{\rm a}) \times \begin{bmatrix} K_1(m^*r_{\rm o})I_0(m^*r) + I_1(m^*r_{\rm o})K_0(m^*r) \\ \overline{K_0(m^*\xi)I_1(m^*r_{\rm o}) + K_1(m^*r_{\rm o})I_0(m^*\xi)} \end{bmatrix} \\ (A13) \\ \frac{dT_{\rm f}}{dr} \bigg|_{r=\xi^+} &= (T_{\rm dew} - T_{\rm a})m^* \begin{bmatrix} K_1(m^*r_{\rm o})I_1(m^*\xi) - I_1(m^*r_{\rm o})K_1(m^*\xi) \\ \overline{K_0(m^*\xi)I_1(m^*r_{\rm o}) + K_1(m^*r_{\rm o})I_0(m^*\xi)} \end{bmatrix} \\ (A14) \end{split}$$

where

$$m^{*^2} = \frac{2h_{\rm s}}{k_{\rm f} \cdot \delta_{\rm f}} \tag{A15}$$

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